

Experimentally Validated Simulator of Flight Dynamics: for a Magnus Effect-based Quadcopter System

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ABSTRACT

Unmanned aerial vehicles (UAVs) have gained extensive utilization across diverse industries, necessitating the enhancement of their capabilities through addressing their power consumption limitations. In this context, the Magnus effect can increase UAV autonomy by exploiting its aerodynamic capabilities. The presented study contributes a reliable 6-DoF nonlinear simulator tailored for a drone equipped with Magnus cylinders system. Through the execution of experimental flights, the simulator's performance is rigorously validated, establishing its reliability for future deployments.

keywords: Flight Dynamics Simulator, Flight Dynamics Modeling, Experimental Validations, Quadcopters, Magnus Effect.

1 INTRODUCTION

Recent years have seen the use of unmanned aerial vehicles (UAVs) is becoming increasingly prevalent across a wide range of industries and applications. One can cite industrial surveillance [1], infrastructure inspections [2], cinematography [3], merchandise transport [4] or aerial manipulation [5]. It is an ongoing challenge to develop UAVs that can fly longer distances and perform more complex tasks, and their power consumption is one of the main factors affecting their range and endurance. To address this issue, researchers have been exploring various methods for reducing UAVs energy consumption. In recent years, there has been renewed interest in the Magnus effect, which has been known for over a century [6], but has gained renewed attention in light of its potential application to UAVs [7, 8]. With Magnus cylinders attached to UAVs, lift can be generated without the use of traditional flight controls such as flaps or rudders, and flight trajectory can be controlled more precisely and flexibly.

Magnus cylinders offer several advantages over traditional control surfaces. These include that the speed and direction of rotation of the cylinders may be controlled robustly in order to create the desired aerodynamic forces, thereby providing greater control over the flight path of an aircraft. The Magnus effect can also reduce power consumption as it generates lift, which help maintain altitude, reducing the amount of power required to maintain the UAV's altitude. This is particularly relevant for UAVs that fly long distances over extended periods of time, such as those used in search

and rescue missions, etc. Overall, the Magnus effect has the potential to improve UAV technology by providing enhanced control and reducing energy consumption.

In this context, the presented study aims to develop a reliable 6-DoF nonlinear simulator for the quadcopter with the Magnus cylinder system. This will provide a comprehensive description of the system and help in the design of future autopilots in the applications of airborne wind energy production [9, 10].

Paper Organisation : Firstly, Section 2 addresses the flight mechanics model of the Magnus based quadcopter. It begins by presenting the equations of motion, covering both translational and rotational dynamics. In Section 3, a detailed explanation of all the forces and torques acting on the system is provided. The design of the PID based position control strategy is explained in Section 4. Moving on, Section 5 provides a brief description of the experimental setup used for validating the simulator. Finally, Section 6 presents an overview of the overall simulator along with the reliability study and simulator validation through analysing and comparing some simulations and experimental flight results.

Notations : for the seek of clarity, a series of notations is defined. For vector $\mathbf{x}$, we denote by $\|\mathbf{x}\|$ the $\mathcal{L}_2$ norm of $\mathbf{x}$ and by $\bar{\mathbf{x}}$ its transpose. $[\mathbf{x}]^{\mathcal{A}}$ is the representation of $\mathbf{x}$ expressed in $\mathcal{A}$ coordinate frame and $D^{\mathcal{A}}\mathbf{x}$ its derivative w.r.t frame $\mathcal{A}$. Regarding the dynamics, $\mathbf{s}_{BA}$ denotes the displacement vector of point B w.r.t point A , on the other hand, $\mathbf{S}_{BA}$ represents the skew matrix of the position vector $\mathbf{s}_{BA}$. Vector $\mathbf{v}_B^{\mathcal{A}}$ represents the linear velocity of point mass B w.r.t $\mathcal{A}$ coordinate frame and $\boldsymbol{\omega}^{\mathcal{B},\mathcal{A}}$ is the angular velocity vector of frame $\mathcal{B}$ w.r.t frame $\mathcal{A}$. Given an angle θ we denote c_θ , s_θ , and t_θ to the cosine, sin, and tangent of θ .

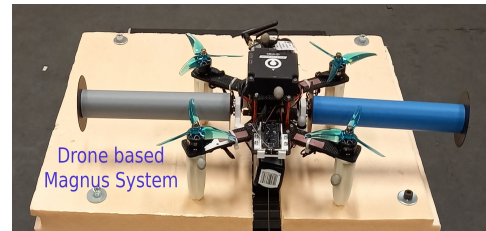


Figure 1: Magnus Effect-based Quadcopter prototype.

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2 NONLINEAR FLIGHT MECHANICS MODEL

The Magnus based quadcopter system consists of a quadrotor drone and two spinning Magnus cylinders connected to the right and left of the drone respectively as shown in Fig. 1. Table 1, represents the involved parameters of the system. The standard flight mechanics theory [11] is used to derive the 6-DoF nonlinear dynamics that govern the behavior of the system. All the following parameters and equations are used and coded in MATLAB/Simulink, to form the core of the realistic Magnus Effect-based Quadcopter System Simulator. The following reference frames are defined to formulate the equations of motion,

- Inertial Frame $\mathcal{I}(\mathbf{i}_1, \mathbf{i}_2, \mathbf{i}_3)$: Its base point I is assumed to be the reference of the position measurements.
- Drone Body Frame $\mathcal{D}'(\mathbf{d}_1, \mathbf{d}_2, \mathbf{d}_3)$: Its base point coincides with the drone's center of mass D . The base vectors $\mathbf{d}_1$, $\mathbf{d}_2$, and $\mathbf{d}_3$ are aligned with the principle axes of the moment of inertia, such that $\mathbf{d}_3$ is directed upwards.
- Right Magnus Frame $\mathcal{M}_r(\mathbf{m}_{r1}, \mathbf{m}_{r2}, \mathbf{m}_{r3})$: Its base point coincides with the right Magnus wing center of mass M_r . The base vector $\mathbf{m}_{r2}$ is aligned with the right Magnus cylinder axis of rotations.
- Left Magnus Frame $\mathcal{M}_l(\mathbf{m}_{l1}, \mathbf{m}_{l2}, \mathbf{m}_{l3})$: Its base point coincides with the left Magnus wing center of mass M_l . The base vector $\mathbf{m}_{l2}$ is aligned with the left Magnus cylinder axis of rotations.
- System Body Frame $\mathcal{D}(\mathbf{d}_1, \mathbf{d}_2, \mathbf{d}_3)$: Its base point coincides with the system drone+Magnus's center of mass C . The base vectors are parallel to that of $\mathcal{D}'$. This frame is considered as the body frame supporting all other spinning bodies.

The rotation matrix in this flight mechanics $\mathbf{R}^{\mathcal{D}\mathcal{I}}$ is the one of system frame $\mathcal{D}$ w.r.t inertial frame $\mathcal{I}$. It is composed of three rotations by the so-called Euler angles: roll, pitch, yaw or ϕ , θ and ψ . In our simulator, we use quaternions instead of Euler angles to represent the drone's rotation, as quaternions avoid the problem of gimbal lock and are more computationally efficient. The rotation quaternion is represented by the four dimensional coordinates $\bar{q} = [q_0 \ q_1 \ q_2 \ q_3]$.

Parameter	Description	Value
m	Total mass	1.568 kg
m_D	Drone mass	1.47 kg
m_{M_k}	kth Magnus mass	0.049 kg
L_{M_k}	kth Magnus length	0.179 m
R_{M_k}	kth Magnus radius	0.0175 m

Table 1: Model Parameters

It is assumed that the two unit directions $\mathbf{m}_{r2}$ and $\mathbf{m}_{l2}$ are collinear and they are parallel to $\mathbf{d}_2$ with an offset along $\mathbf{d}_3$ of δ_z such that,

$$[\overline{\mathbf{s}_{M_r D}}]^{\mathcal{D}} = \begin{bmatrix} 0 & \frac{L_r}{2} & -\delta_z \end{bmatrix}, \quad [\overline{\mathbf{s}_{M_l D}}]^{\mathcal{D}} = \begin{bmatrix} 0 & -\frac{L_l}{2} & -\delta_z \end{bmatrix} \quad (2.1)$$

The common center of mass C can be determined as follows,

$$[\mathbf{s}_{CD}]^{\mathcal{D}} = \frac{\sum_k m_{M_k} [\mathbf{s}_{M_k D}]^{\mathcal{D}}}{m} \quad (2.2)$$

2.1 System Mathematical Model

First, it is important to mention that the centers of mass are mutually fixed. The translational and attitude dynamic equations are formulated using Newton's and Euler's laws of clustered bodies, respectively:

$$m \mathbf{D}^{\mathcal{I}} \mathbf{v}_C^{\mathcal{I}} = \mathbf{F}_C + \mathbf{F}_D + \sum_k \mathbf{F}_{M_k} + \mathbf{P} \quad (2.3)$$

$$\begin{aligned} & \mathbf{D}^{\mathcal{I}} (\mathbf{I}_D^{\mathcal{D}} \mathbf{w}^{\mathcal{D}\mathcal{I}}) + \mathbf{D}^{\mathcal{I}} (m_D \overline{\mathbf{S}}_{DC} \mathbf{S}_{DC} \mathbf{w}^{\mathcal{D}\mathcal{I}}) + \sum_k \mathbf{D}^{\mathcal{I}} (\mathbf{I}_{M_k}^{\mathcal{M}_k} \mathbf{w}^{\mathcal{M}_k \mathcal{I}}) \\ & + \sum_k \mathbf{D}^{\mathcal{I}} (m_{M_k} \overline{\mathbf{S}}_{M_k C} \mathbf{S}_{M_k C} \mathbf{w}^{\mathcal{M}_k \mathcal{I}}) = \mathbf{\Gamma}_C + \mathbf{\Gamma}_D + \sum_k \mathbf{\Gamma}_{M_k} \end{aligned} \quad (2.4)$$

where $k \in \{r, l\}$ represents the dynamics of the right and left Magnus separately and $\mathbf{P} = m\mathbf{g}$ is the system weight. The force vectors $\mathbf{F}_D$ and $\mathbf{F}_{M_k}$ are the total forces exerted on the system due to the drone propellers and Magnus cylinders respectively. Similarly, $\mathbf{\Gamma}_D$ and $\mathbf{\Gamma}_{M_k}$ are the torques acting on the system due to the drone propellers and Magnus cylinders respectively. However, the force vector $\mathbf{F}_C$ and the torque vector $\mathbf{\Gamma}_C$ are the additional control contribution. The detailed derivation of these forces and torques vectors will be represented in the next sections.

The angular velocity dynamics can be derived from (2.4) by

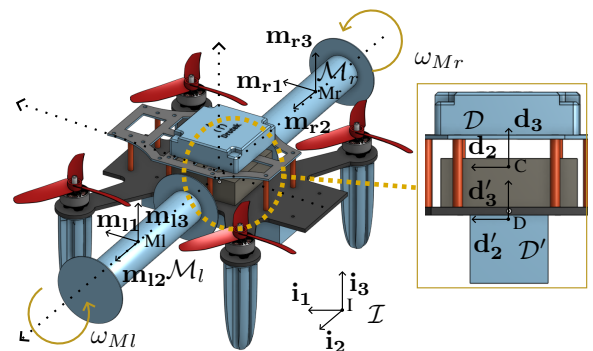


Figure 2: Frame definition on the quadcopter. From figure, $\mathcal{D}$ represents the body frame, $\mathcal{D}'$ the drone body frame, $\mathcal{M}_l$ the left Magnus frame, $\mathcal{M}_r$ the right Magnus frame and eventually $\mathcal{I}$ the inertial frame.

transferring the rotational derivative to the frame of the main body $\mathcal{D}$. We can deduce,

$$\begin{aligned} J D^{\mathcal{D}} \mathbf{w}^{\mathcal{D}\mathcal{I}} &= -\Omega^{\mathcal{D}\mathcal{I}} J \mathbf{w}^{\mathcal{D}\mathcal{I}} + \Gamma_C + \Gamma_D + \sum_k \Gamma_{M_k} \\ &- \sum_k (\Omega^{\mathcal{D}\mathcal{I}} \mathbf{I}_{M_k}^{\mathcal{M}_k} \mathbf{w}^{\mathcal{M}_k\mathcal{D}}) - \sum_k (\mathbf{I}_{M_k}^{\mathcal{M}_k} D^{\mathcal{D}} \mathbf{w}^{\mathcal{M}_k\mathcal{D}}) \end{aligned} \quad (2.5)$$

such that:

$$\begin{cases} \mathbf{J}_D^{\mathcal{D}} = \mathbf{I}_D^{\mathcal{D}'} + m_D \bar{\mathbf{S}}_{DC} \mathbf{S}_{DC} \\ \mathbf{J}_M^{\mathcal{D}} = \sum_k (\mathbf{I}_{M_k}^{\mathcal{M}_k} + m_{M_k} \bar{\mathbf{S}}_{M_k C} \mathbf{S}_{M_k C}), \\ \mathbf{J} = \mathbf{J}_D^{\mathcal{D}} + \mathbf{J}_M^{\mathcal{D}} \end{cases} \quad (2.6)$$

The revolving angular velocity vectors and the moment of inertia matrix of each Magnus cylinder about its axis of symmetry, are expressed as,

$$[\mathbf{w}^{\mathcal{M}_k\mathcal{D}}]^{\mathcal{D}} = \begin{bmatrix} 0 \\ w_{M_k} \\ 0 \end{bmatrix}, [\mathbf{I}_{M_k}^{\mathcal{M}_k}]^{\mathcal{D}} = \begin{bmatrix} I X_k & 0 & 0 \\ 0 & I Y_k & 0 \\ 0 & 0 & I X_k \end{bmatrix} \quad (2.7)$$

As a result, the translational and attitude dynamic state variables correspond to frame $\mathcal{D}$'s linear and angular velocities w.r.t. frame $\mathcal{I}$, respectively:

$$[\mathbf{v}_C^{\mathcal{I}}]^{\mathcal{I}} = [\dot{\mathbf{s}}_{CI}]^{\mathcal{I}} = \begin{bmatrix} \dot{x} \\ y \\ z \end{bmatrix}, [\mathbf{w}^{\mathcal{D}\mathcal{I}}]^{\mathcal{D}} = \begin{bmatrix} p \\ q \\ r \end{bmatrix} \quad (2.8)$$

Moreover, the skew matrix of the angular velocity vector $\mathbf{w}^{\mathcal{D}\mathcal{I}}$ and the drone moment of inertia are expressed as:

$$\begin{aligned} [\Omega^{\mathcal{D}\mathcal{I}}]^{\mathcal{D}} &= \begin{bmatrix} 0 & -r & q \\ r & 0 & -p \\ -q & p & 0 \end{bmatrix}, \\ [\mathbf{I}_D^{\mathcal{D}'}]^{\mathcal{D}} &= \begin{bmatrix} I X & I X Y & I X Z \\ I X Y & I Y & I Y Z \\ I X Z & I Y Z & I Z \end{bmatrix} \end{aligned} \quad (2.9)$$

The equation of angular position can be expressed in terms of angular velocities $\mathbf{w}^{\mathcal{D}\mathcal{I}}$ expressed in $\mathcal{D}$. Based on the Euler ZYX formalism,

$$\begin{cases} \dot{\Theta} = \begin{bmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{bmatrix} = \mathbf{W}^{-1} \mathbf{w}^{\mathcal{D}\mathcal{I}} \\ \mathbf{W}^{-1} = \begin{bmatrix} 1 & s_{\phi} t_{\theta} & c_{\phi} t_{\theta} \\ 0 & c_{\phi} & -s_{\phi} \\ 0 & s_{\phi}/c_{\theta} & c_{\phi}/c_{\theta} \end{bmatrix} \end{cases} \quad (2.10)$$

with $\mathbf{W}$ known as the Wronskien matrix of the Euler angles Θ attitude representation. The quaternion formalism of the angles' dynamics is obtained as follows,

$$\dot{\mathbf{q}} = \frac{1}{2} \begin{bmatrix} 0 & -\overline{\mathbf{w}^{\mathcal{D}\mathcal{I}}} \\ \mathbf{w}^{\mathcal{D}\mathcal{I}} & \Omega^{\mathcal{D}\mathcal{I}} \end{bmatrix} \mathbf{q} \quad (2.11)$$

3 FORCES AND TORQUES

3.1 Actuator dynamics

The presented system uses six brushless motors as actuators. Each one of which is modeled in this work by its single-phase electro-mechanical equivalent model, defined as follows for w the motor rotation speed :

$$\begin{cases} J_r \dot{\omega} &= \Gamma_{mot} - \Gamma_{res} \\ U &= \text{sat}(e + RI + LI) \end{cases} \quad (3.1)$$

Where J_r represents the inertia of the motor and load (Magnus or propeller) assembly. U , e and I are respectively referring to the motor phase voltage, the electromechanical force and the phase current. The phase resistance R and inductance L are directly measured on the motor. Motor torque Γ_{mot} is proportional to the phase current by electric constant K_c . Electromechanical force is proportional to the rotation speed through mechanical constant K_m . Resistive torque Γ_{res} can be approximated as the sum of an air friction quadratic torque, with C_Q the drag coefficient of the motor load, and a mechanical dry friction $\alpha\omega$:

$$\begin{cases} \Gamma_{mot} &= K_c I \\ \Gamma_{res} &= C_Q \omega^2 + \alpha\omega \\ e &= K_m \omega \end{cases} \quad (3.2)$$

In the rest of this paper, ω_{R_i} will refer to each propeller equipped motor $i \in \{1, 2, 3, 4\}$ rotation speed, and $\omega_{\mathcal{M}_k}$ to the Magnus cylinder equipped motor $k \in \{r, l\}$.

3.2 Drone Forces:

- The forces applied to the system by the four propellers $i \in \{1, 2, 3, 4\}$ are :

$$\mathbf{F}_{R_i}^m = C_T \|\mathbf{w}^{\mathcal{R}_i\mathcal{D}}\| \mathbf{w}^{\mathcal{R}_i\mathcal{D}} \quad (3.3)$$

with C_T generalized thrust coefficient and $\mathbf{w}^{\mathcal{R}_i\mathcal{D}}$ is the angular velocity vector of each rotor i such that,

$$\mathbf{w}^{\mathcal{R}_i\mathcal{D}} = w_{R_i} \mathbf{d}_3 \quad (3.4)$$

Therefore, the total thrust force exerted by the four propellers is

$$\mathbf{F}_D^m = \sum_i \mathbf{F}_{R_i}^m \quad (3.5)$$

- The aerodynamic forces due to its motion through the apparent wind speed, which is computed as

$$\mathbf{v}_a = \mathbf{v}_w - \mathbf{v}_C^{\mathcal{I}} \quad (3.6)$$

with $\mathbf{v}_w$ is the wind velocity vector.

We consider here only the aerodynamic drag forces of drone's body

$$\mathbf{F}_D^a = \frac{1}{2} \rho C_D \|\mathbf{v}_a\|^2 \mathbf{S} \quad (3.7)$$

with C_D is the drone's drag coefficient and $\mathbf{S}$ is the drone's exposed surface vector.

3.3 Magnus Forces:

The aerodynamic characteristics of the Magnus cylinder is affected by various factors. The most important one that controls Magnus effect-based wing is its spin ratio X which is the ratio between the local tangential velocity and the apparent wind velocity v_a , such that for each Magnus wing $k \in \{r, l\}$

$$X_k = \frac{R_{M_k} \|\mathbf{w}^{\mathcal{M}_k \mathcal{D}}\|}{\|\mathbf{v}_a\|} \quad (3.8)$$

In this work, we chose to add endplates to the two Magnus cylinders. This can significantly enhance lift and improve the lift-to-drag ratio while maintaining small aspect ratio $\Lambda = 5.1$. The endplates diameter was chosen to be twice that of the Magnus cylinder. The drag and lift coefficients dynamics are extracted from the wind tunnel tests gathered and analysed in [12]. These forces can be derived as follows:

$$\begin{aligned} \mathbf{F}_{M_k}^D &= \frac{1}{2} \rho C_{D_k} S_{M_k} \|\mathbf{v}_{a_k}\|^2 \mathbf{e}_{D_k} \\ \mathbf{F}_{M_k}^L &= \frac{1}{2} \rho C_{L_k} S_{M_k} \|\mathbf{v}_{a_k}\|^2 \mathbf{e}_{L_k} \end{aligned} \quad (3.9)$$

such that S_{M_k} represents the projected surface area of each $k \in \{r, l\}$ Magnus cylinder and the aerodynamic drag and lift coefficient of the right and left Magnus cylinders are as follows:

$$\begin{cases} C_{D_k} := C_{D_k}(\mathbf{w}^{\mathcal{M}_k \mathcal{D}}, \|\mathbf{v}_{a_k}\|) \\ C_{L_k} := C_{L_k}(\mathbf{w}^{\mathcal{M}_k \mathcal{D}}, \|\mathbf{v}_{a_k}\|) \end{cases} \quad (3.10)$$

The apparent wind velocity experienced by right and left cylinders at their respective center of mass M_r and M_l respectively are:

$$\begin{aligned} \mathbf{v}_{a_r} &= \mathbf{v}_a + \frac{L_{M_r}}{2} r \mathbf{d}_1 \\ \mathbf{v}_{a_l} &= \mathbf{v}_a - \frac{L_{M_l}}{2} r \mathbf{d}_1 \end{aligned} \quad (3.11)$$

The directions of the drag and lift forces for each Magnus wings $i \in \{r, l\}$ is defined such that the drag force is in the direction of the apparent wind velocity and the lift force is orthogonal to the Magnus wing axis of rotation and to the apparent wind velocity, then we deduce:

$$\begin{cases} \mathbf{e}_{D_k} = \frac{[\mathbf{v}_{a_k}]^{\mathcal{D}}}{\|\mathbf{v}_{a_k}\|} \\ \mathbf{e}_{L_k} = \mathbf{m}_{k2} \times \mathbf{e}_{D_k} \end{cases} \quad (3.12)$$

Hence, the total aerodynamic forces of each Magnus wing is read as:

$$\begin{cases} \mathbf{F}_{M_r}^a = \mathbf{F}_{M_r}^D + \mathbf{F}_{M_r}^L \\ \mathbf{F}_{M_l}^a = \mathbf{F}_{M_l}^D + \mathbf{F}_{M_l}^L \end{cases} \quad (3.13)$$

3.4 Total Forces:

We can deduce the total forces applied to the system, in inertial frame $\mathcal{I}$, based on (3.3)-(3.13) as follows:

$$\begin{aligned} \mathbf{F}_C &= \mathbf{R}^{\mathcal{DI}} \mathbf{F}_D^m \\ \mathbf{F}_D &= \mathbf{R}^{\mathcal{DI}} \mathbf{F}_D^a \\ \sum_k \mathbf{F}_{M_k} &= \mathbf{R}^{\mathcal{DI}} (\mathbf{F}_{M_r}^a + \mathbf{F}_{M_l}^a) \end{aligned} \quad (3.14)$$

3.5 Drone torques:

- Spinning drone torque:

The drone yaw torque is defined as follows,

$$\Gamma_D^y = \sum_i (C_Q \|\mathbf{w}^{\mathcal{R}_i \mathcal{D}}\| \mathbf{w}^{\mathcal{R}_i \mathcal{D}})$$

such that C_Q is the propeller's drag coefficient.

- Torque induced by drone's motors thrust forces is computed as follows:

$$\Gamma_D^m = \sum_i (\mathbf{s}_{R_i C} \times \mathbf{F}_{R_i}^m) \quad (3.15)$$

where $\mathbf{s}_{R_i C}$ for $i \in \{1, 2, 3, 4\}$ specifies the drone's geometry.

- Gyroscopic Effect drone torques:

As the drone's rotors $\mathcal{R}_i$ for $i \in \{1, 2, 3, 4\}$ is spinning around $\mathbf{d}_3$, then if the system is rolling or pitching, a gyroscopic torque is resulted as follows:

$$\Gamma_D^g = I_r \sum_i (\mathbf{w}^{\mathcal{R}_i \mathcal{D}} \times \mathbf{w}^{\mathcal{DI}}) \quad (3.16)$$

with I_r is the rotor and propeller moment of inertia.

- Inertial rotation torque:

$$\Gamma_D^i = -I_r \sum_i (D^{\mathcal{D}} \mathbf{w}^{\mathcal{R}_i \mathcal{D}}) \quad (3.17)$$

3.6 Magnus torques:

- Spinning torque:

The Magnus cylinder pitch torque is defined as follows,

$$\Gamma_M^p = \sum_k (C_{Q_k} \|\mathbf{w}^{\mathcal{M}_k \mathcal{D}}\| \mathbf{w}^{\mathcal{M}_k \mathcal{D}}) \quad (3.18)$$

such that $C_{Q_k} = \frac{1}{2} \rho \pi C_f S_{M_k} R_{M_k}^3$ and C_f is the skin friction coefficient of cylinder surface [13].

- Magnus cylinder Aerodynamic torques: torques arise due to the difference between the lift and drag produced by each cylinder and is expressed as:

$$\begin{cases} \Gamma_{M_r}^a = \mathbf{s}_{M_r C} \times \mathbf{F}_{M_r}^a \\ \Gamma_{M_l}^a = \mathbf{s}_{M_l C} \times \mathbf{F}_{M_l}^a \\ \Gamma_M^a = \Gamma_{M_r}^a + \Gamma_{M_l}^a \end{cases} \quad (3.19)$$

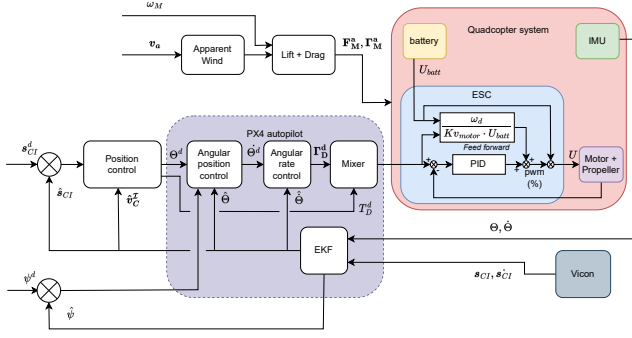


Figure 3: Magnus based quadcopter control architecture

- Gyroscopic Effect and inertial Magnus torques: We can see from (2.5) that the last two terms represent respectively the gyroscopic and inertial rotation torques of the two Magnus cylinders such that

$$\begin{aligned}\Gamma_M^g &= -\sum_k (\Omega^{DI} I_{M_k}^{\mathcal{M}_k} \omega^{\mathcal{M}_k \mathcal{D}}) \\ \Gamma_M^i &= -\sum_k (I_{M_k}^{\mathcal{M}_k} D^{\mathcal{D}} \omega^{\mathcal{M}_k \mathcal{D}})\end{aligned}\quad (3.20)$$

3.7 Total torques:

Torques from (3.20) could be included in torques exerted by Magnus cylinders and thus the angular velocity dynamics (2.5) can be simplified,

$$JD^{\mathcal{D}} \omega^{\mathcal{D}\mathcal{I}} = -\Omega^{\mathcal{D}\mathcal{I}} J \omega^{\mathcal{D}\mathcal{I}} + \Gamma_C + \Gamma_D + \sum_k \Gamma_{M_k} \quad (3.21)$$

Therefore, we can deduce the total torques applied to the system, in body frame $\mathcal{D}$, based on (3.16)-(3.15) as follows:

$$\begin{aligned}\Gamma_C &= \Gamma_D^y + \Gamma_D^m \\ \Gamma_D &= \Gamma_D^g + \Gamma_D^i \\ \sum_k \Gamma_{M_k} &= \Gamma_M^p + \Gamma_M^a + \Gamma_M^g + \Gamma_M^i\end{aligned}\quad (3.22)$$

4 CONTROL STRATEGY

In this section we present the design of the overall control strategy. The control strategy is based on simplified model of the system. This simplified model comes from a simplification of the complete nonlinear model, described in sections (2.3) and (3.21), in which aerodynamic effects, ground effect and gyroscopic effects are neglected. This model is described as follows:

$$\begin{cases} \dot{s}_{CI} &= v_C^{\mathcal{I}} \\ m \dot{v}_C^{\mathcal{I}} &= F_C + P \\ \dot{\Theta} &= W^{-1} \omega^{\mathcal{D}\mathcal{I}} \\ J \dot{\omega}^{\mathcal{D}\mathcal{I}} &= -\Omega^{\mathcal{D}\mathcal{I}} J \omega^{\mathcal{D}\mathcal{I}} + \Gamma_C \end{cases} \quad (4.1)$$

4.1 Position and Velocity Loop:

The system's position and velocity can be controlled by F_C . The latest is represented by its projections in the inertial frame $\mathcal{I}$: $F_{C_x}, F_{C_y}, F_{C_z}$ that controls x, y, z loops respectively. We have implemented the PID control strategy to compute these control forces, for each loop $q \in \{x, y, z\}$, as follows:

$$F_{C_q} = m(k_{d_q} \dot{q} + k_{p_q} q + k_{i_q} \int e_q d\tau) \quad (4.2)$$

with e_q is the tracking error of each loop $q \in \{x, y, z\}$. The inner loops are fed by the desired thrust force T_D^d and the desired Euler angles Θ^d . These are derived from (4.2) according to the kinematic transformation as follows:

$$\begin{cases} T_D^d &= m(F_{C_x} + g)/(c_\phi c_\theta) \\ \theta^d &= \text{atan2}((F_{C_x} c_\psi + F_{C_y} s_\psi), F_{C_z} + g), \\ \phi^d &= \text{atan2}(c_\theta((F_{C_x} s_\psi - F_{C_y} c_\psi), F_{C_z} + g)\end{cases} \quad (4.3)$$

4.2 Attitude and Angular Velocities Loops:

The simplified model in (4.1), gives a general view about the inner attitude and angular velocities control loops. On one hand, the angular position represented by the Euler angles Θ can be controlled by the angular velocities $\omega^{\mathcal{D}\mathcal{I}}$. On the other hand, the angular velocities $\omega^{\mathcal{D}\mathcal{I}}$ can be controlled by the controller torque Γ_C . We use a PX4 onboard autopilot [14]. This autopilot manages the attitude and angular speed loops. PX4 control structure for rate and attitude loops have been copied in the MATLAB/Simulink simulator, based on in-flight tune control gains and control diagrams given by PX4.

4.3 PX4 Mixers

- PX4 Normalized Mixer: The hover compensation is applied to account for any variations in the drone's hover performance. The normalized desired total thrust force is computed as, $T_D^n = \frac{hc}{mg} T_D$ with hc is the hover compensation factor dependent on the specific drone and its configuration.
- PX4 Identified Mixer: It is based on a linear relationship between torque Γ_C and force T_D commands and the four rotors PWM signals setpoint. It is described as:

$$\begin{bmatrix} \omega_{R_1} \\ \omega_{R_2} \\ \omega_{R_3} \\ \omega_{R_4} \end{bmatrix} = M_{PX4} \begin{bmatrix} \Gamma_C \\ T_D^n \end{bmatrix} \quad (4.4)$$

5 EXPERIMENTAL SETUP

Our custom build quadcopter flies on an Hollybro Pixhawk 4 flight controller running PX4 Autopilot. Offboard position control is performed on a ground station through ROS1. Communication between the UAV and the ground station is performed via Mavlink protocol through Wifi. In order to perform indoor flight as GPS (GNSS receiver) is not available, position measurement is provided by Vicon motion capture system. The UAV is running on a 4S LiPo battery. All material is listed in Table 2 and diagrammed in Figure 4

Brushless motor speed control is performed with an ESC (Electronic Speed Controller). The ESC is meant to apply to the motor a fraction of the battery voltage. This fraction is given by a standard digital input (most generally PWM or Dshot signal). Thus, standard motor control is performed in *open loop* with respect to the desired rotation speed. In practice, air and dry friction cause the motor to run slower than expected. In order to achieve precise speed control, and thus precise force control on each motor, we have implemented a custom firmware into standard ARM32 processor based ESCs allowing *close loop* speed control. In our experimental setup, the input of the ESC is then a desired speed, and not a percentage of battery voltage. In the ESC, speed control is performed through a standard PID regulation in which speed measurement is performed by monitoring the inversion of phase current due to the movement of rotor magnets. The ESC firmware that has been used is available at ¹.

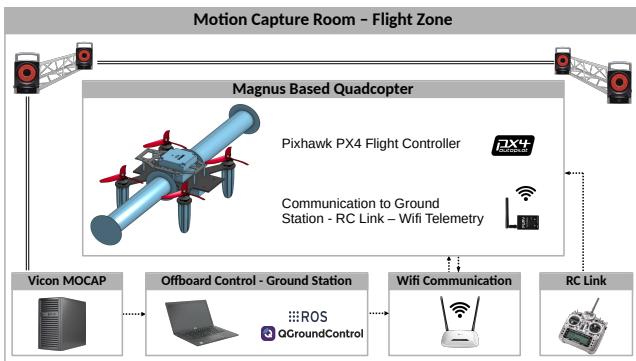


Figure 4: Gipsa-Lab experimental setup

6 RELIABILITY STUDY

To study the reliability of our model we propose a three steps approach to compare flight data to simulated ones. Propulsion model is to be validated with a dedicated protocol detailed in Section 6.1. On a position step scenario with no spinning of the cylinders, we will validate inner loops, inertia and body dynamics. Finally, added gyroscopic effects

¹<https://github.com/gipsa-lab-uav/AM32-MultiRotor-ESC-firmware>

Item	Description
Flight controller	Holybro Pixhawk 4 with PX4 v1.14 firmware
Battery	Bashing 4S 5000mAh
Radiocontroller	FrSky Taranis X9D
RC receiver	FrSky XM+
Motor	T-Motor F60proV 1750 Kv
Propeller	T-Motor T5147
Propeller ESC	HGLRC 4in1 Zeus 45A
Magnus ESC	HGLRC T-Rex 35A
Wifi Communication	ESP32 dev kit with serial/wifi bridge firmware
Motion capture system	12 Vicon T40s cameras, Tracker software

Table 2: Hardware setup

will be assessed under constant cylinder rotation speed scenario. Inertial effects will be shown in the inner attitude and rate loops by changing in flight the rotational speed of the cylinders. Modeling the aerodynamics of the Magnus cylinders' necessitates significant linear and rotational speed testing scenarios which are not performed in this work. In lift and drag aerodynamics are not addressed in this work as they are well documented in literature. We are then focusing on low linear speed scenarios. These torques and forces need significant linear speed and rotational speed. At this stage of the study, we based on the Magnus aerodynamic model already published as stated in Section 3.3. However, as future perspective, this dynamics will be validated during external flights at higher speeds.

6.1 Propulsion model validation

The propulsion model, defined in Section 3.1 as a model of a single-phase motor combined to a 5 inches propeller, has been validated experimentally. As explained in Section 4.3, the PX4 autopilot performs a linear mix between the desired forces from position controller and the desired motor speed fed to the ESC. However, as stated in Section 3.1, the generated force is not linear but proportional to the squared rotation velocity of the propeller.

In our control law, we work with a linear approximation of the thrust around the equilibrium point of hover flight for a given flight mass. In order to experimentally validate propeller model used in (3.3), we maintained the UAV in a hover flight with a position control based on the linear approximation of the thrust. Then, every 10 seconds an additional mass of 60 grams is added to the UAV. We monitored desired motor speeds [rad.s⁻¹] and desired Thrust [N]. Figure 5 shows the experimental validation of the propulsion model and of its linear approximation around the flight mass equilibrium point : the estimation of the thrust as proportional to the sum of squared velocities of propellers matches the actual mass of the UAV, whereas its linear approximation used for control fits with the real value around the real flight mass. The lift

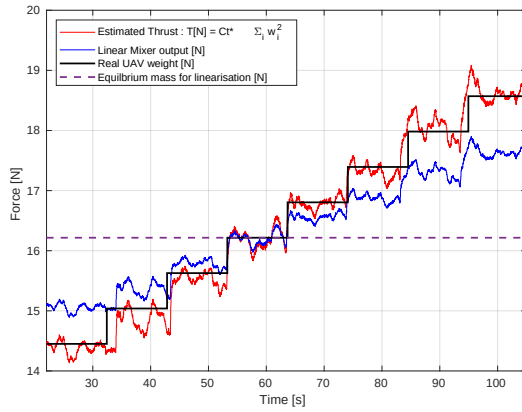


Figure 5: Experimental Thrust model validation

coefficient C_T has been calculated from desired motor speeds and real UAV weight during the protocol.

6.2 Dynamical Model without Magnus rotation

Figures 6, 7, 8 and 9 show comparison between flight data and simulator data of all nested loops dynamics over the same 3D position steps scenario and no cylinder rotation. A yaw step is performed at $t = 110s$. Even if noise level over the angular rates and attitude loops, Figure 6 and 7, are underestimated in the simulator, the main dynamics remains correctly predicted. These noises are mainly due to unmodelled vibrations on the UAV frame, and unmodelled aerodynamics disturbances in an indoor environment (wind turbulence).

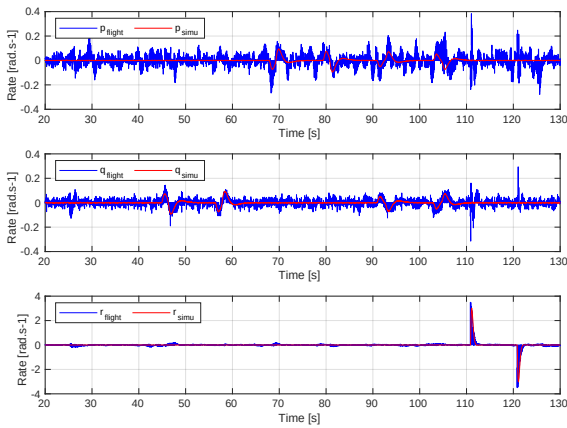


Figure 6: Angular velocities response in case of no Magnus rotation

6.3 Magnus cylinder induced disturbances

- To highlight the gyroscopic effects due to cylinders rotation, let's focus on the effect of a yaw step in hovering flight, at constant cylinder speed $\omega_{M_r} = \omega_{M_l} = 7200\text{rpm}$ over the angular rate p , as shown in Figure 10.

- To highlight the effects of inertia due to cylinder rotation, let's vary cylinder speed in hovering flight between

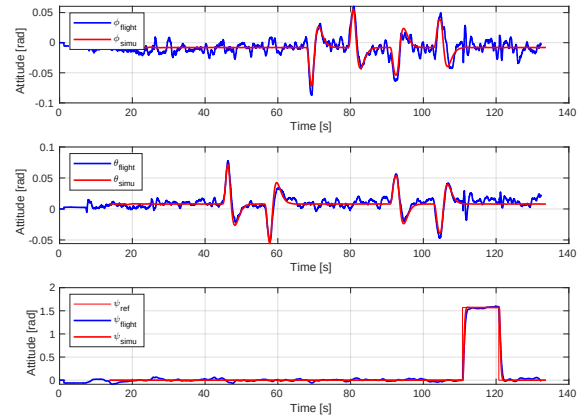


Figure 7: Euler angles response in case of no Magnus rotation

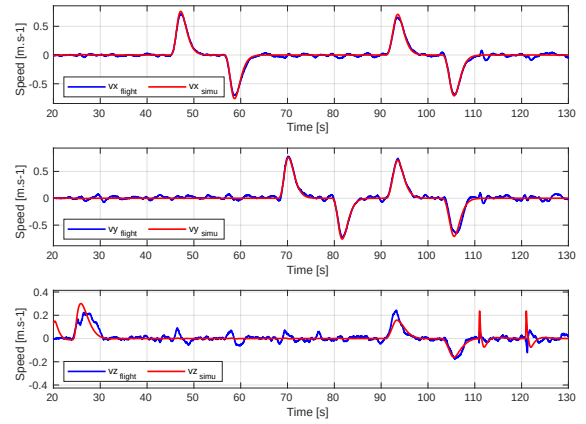


Figure 8: Linear velocities response in case of no Magnus rotation

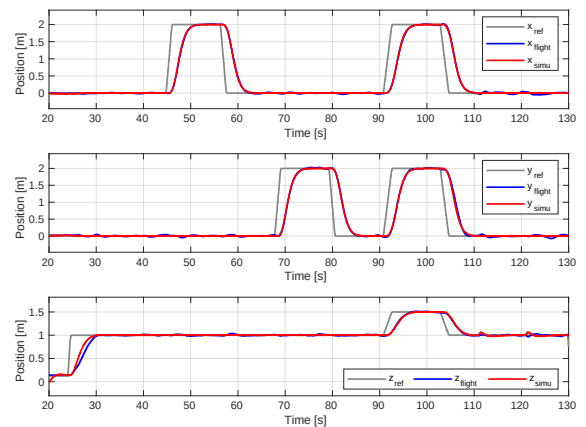
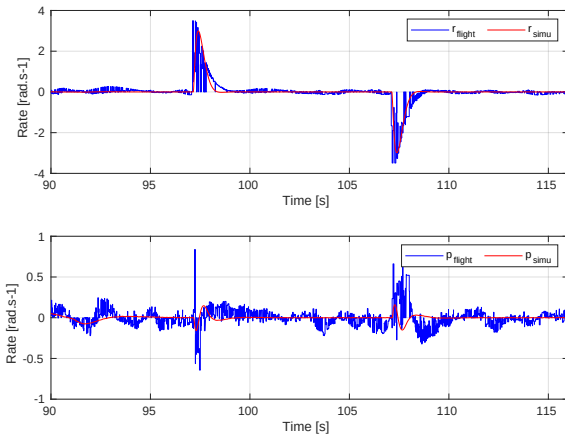
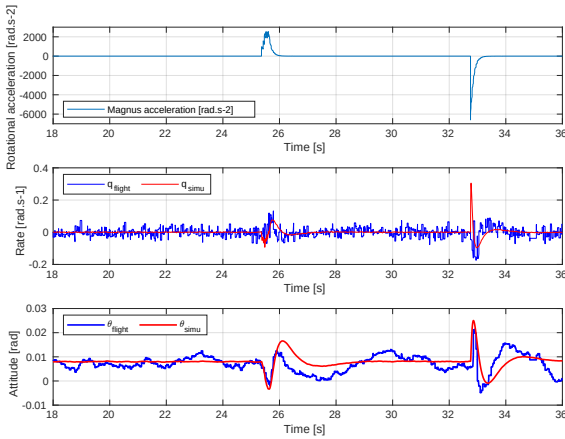


Figure 9: Positions response in case of no Magnus rotation

$\omega_{M_r} = \omega_{M_l} = 5100\text{ rpm}$ (rotations per minutes) and $\omega_{M_r} = \omega_{M_l} = 11400\text{ rpm}$. We simulate and monitor an added inertial torque among the body d_2 axis as shown in Figure 11, on the rate and attitude loops. The acceleration of the cylinders is shown in top of the figure.

Figure 10: Magnus gyroscopic effect on p rateFigure 11: Magnus inertial effects among body d_2 axis

The Magnus rotor friction torque is estimated to be $1.8e - 3$ Nm for maximal speed of rotation 11400 rpm which is negligible regarding to other torques acting on the system.

7 CONCLUSION

This paper presented the design and experimental validation of a 6-DoF simulator for a Magnus-based quadcopter system. This simulator was validated based on flight experimental tests in an indoor environment and loop by loop validation. The results demonstrate that the simulator accurately captures the main dynamics of the system. Its reliability and compatibility with experimental data make it a tool for researchers and engineers to optimize the design and control strategies of Magnus-based quadcopter systems. The findings contribute in the field of Magnus-based quadcopters and enable their use in various industries, paving the way for efficient and capable unmanned aerial vehicles. For future work, it is recommended to incorporate more sensors and Extended Kalman Filter and validate the simulator based on outdoor experiments with higher speeds maneuvers.

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